



**Affiliates Program Meeting 2023**  
**November 8th, 2023**

# Trajectory Informed Multi-fidelity Surrogates for Hypersonic Vehicle Optimization

Jacob Needels (PhD Candidate), Prof. Juan J. Alonso



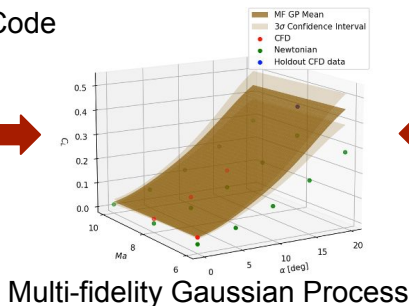
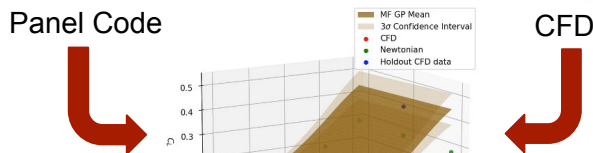
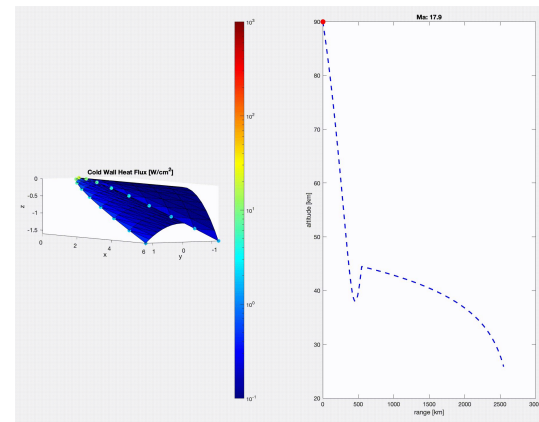
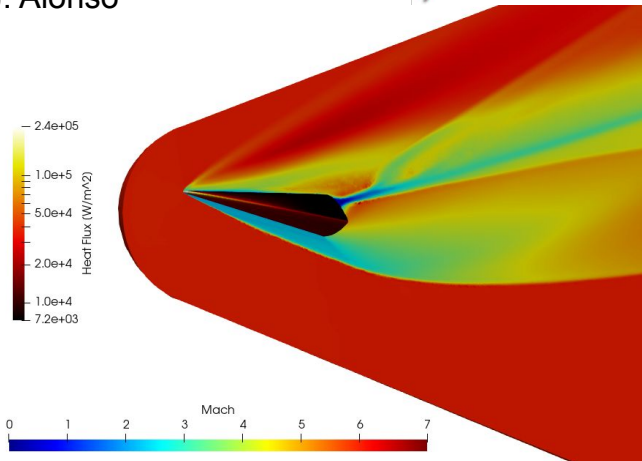
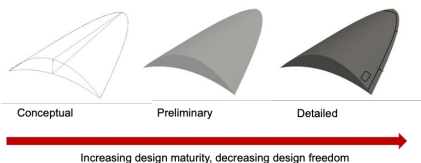
There is always a trade between **accuracy** and **computational cost** in aircraft design, particularly for hypersonic vehicles

**Uncertainties and/or biases** in conceptual design tools can result in **risk to performance and closure** in later design stages

Multi-fidelity methods can **“correct”** **low-fidelity** models using a **small number** of high-fidelity samples, to improve accuracy for minimal cost

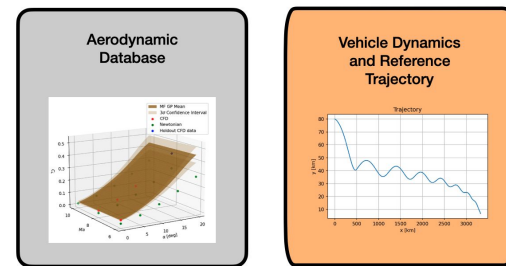
We focus on **improving the information state in conceptual design** while maintaining **tractable computational cost** through:

- **Multi-fidelity Gaussian Process surrogates** of aerodynamic/aerothermal loads, incorporating **model uncertainties**
- **Adjoint-based sensitivity analysis** to guide **sampling** and improve surrogate accuracy for mission-based objectives
- **Multidisciplinary vehicle-trajectory co-design and optimization**



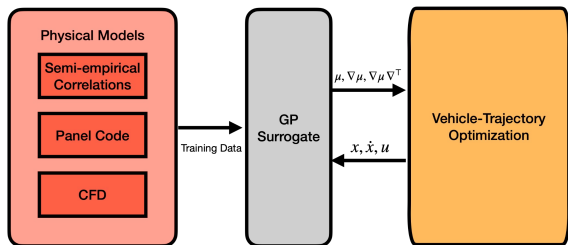
Model	Fidelity	Uncertainty	Cost
SU2	High	±4%	$\mathcal{O}(\text{cpu-hour})$
SHARPE	Low	±20%	≈ 1 cpu-sec

$$\mu, \nabla \mu, \dots \sim \mathcal{L}\mathcal{P}(m, k)$$



$$\delta J = \lambda^T R(x_{ss}, A + \delta A) \delta t$$

Adjoint-based trajectory sensitivities inform sampling



## Bio-Inspired Sensing

Distributed Nerve Endings

Distributed Sensor Network

## Biology

*Biology*

## Fly-by-feel Aircraft

*Fly-by-feel Aircraft*

## Bio-Inspired State Perception

Stall?

AoA  
Airspeed

Function:  $u$   
 $V_\infty$   
 $\alpha$

Operator:  $G(u|y)$

Branch  $_p$

Branch  $_t$

Trunk

Domain:  $y$   
 $\mathbf{x}$

$G_1$

$G_2$

$p$

$\tau$

Data Loss  $L$

Neural Methods for Processing Sensor Data



# An Interdisciplinary Investigation of Hypervelocity Impact Plasmas

Nancy Diallo (PhD Student), Raymond Lau (PhD Candidate), Dr. Nicolas Lee, and Prof. Sigrid Elschot

Figure 1:  
Depiction of  
HVI Plasma  
Expansion  
Process

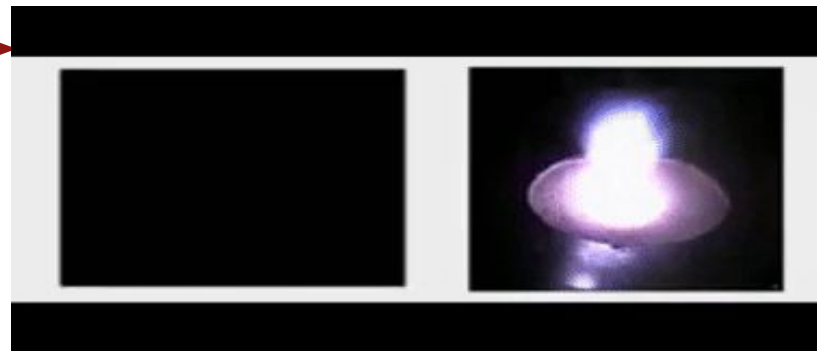
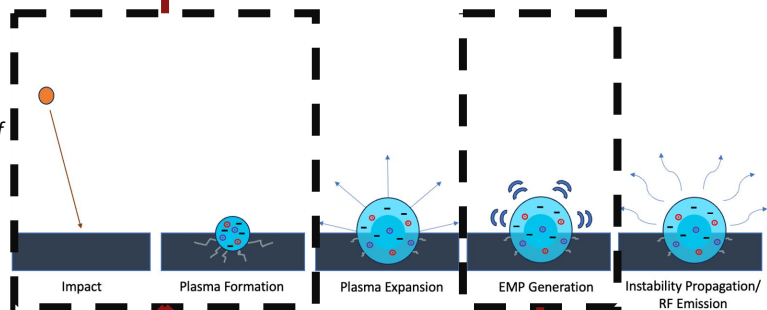
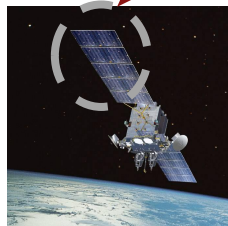


Figure 2: Optical flashes from projectile impacts on a metallic target



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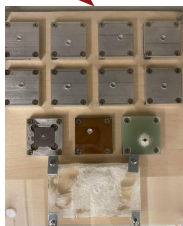


Figure 4:  
Damaged Targets  
from HVI  
Experiments



Figure 3: Charge density  $\rho$ , Electric fields  $E_x$  and  $E_y$ , and magnetic field  $B_z$



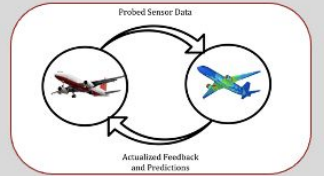
# Physics-Based Digital Twins of Engineering Systems

Marie Jo Azzi<sup>1</sup>, Charbel Farhat<sup>2,3</sup>

Department of Mechanical Engineering, Stanford University  
Department of Aeronautics and Astronautics, Stanford University  
Institute for Computational Mathematics and Engineering, Stanford University

Marie-Jo Azzi  
PhD Candidate  
Farhat Research Group  
(FRG)  
Advisor: Charbel Farhat

## What is a Digital Twin?



- **Digital twin prototype (DTP)**  
Replica of a physical asset/system before it is manufactured. Serves design/analysis purposes.
- **Digital twin instance (DTI)**  
Replica of a physical asset/system after it has been manufactured. Updated in real time to assist with operations (e.g. predictive maintenance).

## Surrogate Models: Internal vs External

- **External models (data-driven)**  
Few, pre-determined, scalar quantities of interest (QoIs). Real-time, surrogate models of output (s). Gaussian processes, artificial neural networks, ...
- **Internal models (physics-based)**  
Arbitrary number of scalar and vector QoIs that can be discovered using the constructed surrogate model. Real-time, surrogate model of system. Projection-based reduced-order models.  
*\*How to identify the QoIs (rare events, failure modes ...)?\**

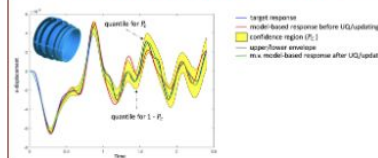
## Model-Form Uncertainty (MFU)

- **MFU inherent to computational model**  
Lack of knowledge of the true physics underlying the problem of interest. Omission or truncation of modeling details.
- **MFU inherent to surrogate model**  
Typical methods for UO involve stochastic computations (e.g. Monte Carlo realizations). Surrogate models typically adopted to achieve computational tractability → additional MFU

## Requirements for a DT

- **High-fidelity modeling**, whether data-driven or physics-based.
- **Modeling and quantifying uncertainty**, and particularly those due to both aforementioned sources of MFU
- **Model Updating**, using a nonparametric stochastic approach.

## Key Performance Indicators



## NPM for Modeling and Quantifying MFU

- NPM randomizes the subspace in which the solution is approximated: Operates at the level of the HPRoM instead of that of the HDM to achieve computational tractability.
- Substitutes the deterministic ROB  $\mathbf{I}^T$  with a stochastic counterpart  $\mathbf{V}(\alpha)$ , where  $\alpha$  is a vector-valued hyperparameter → hyperparameterized ROB and HPRoM. Desired properties of the stochastic ROB:
  - $\mathbf{V}(\alpha)$  is global.
  - $\mathbf{V}(\alpha)$  is random with a probability distribution constructed using MaxEnt.
  - Linear independence of the column is enforced by ensuring that  $\mathbf{V}^T(\alpha)\mathbf{Q}\mathbf{V}(\alpha) = \mathbf{I}$  → NPM constructs the probability measure of  $\mathbf{V}(\alpha)$  on a compact Stiefel manifold
- Enrichment with data via inverse statistical problem
- Identification of hyperparameter vector  $\alpha$

$$\alpha^{opt} = \arg \min_{\alpha} J(\alpha)$$

$$J(\alpha) = w_n J_{new}(\alpha) + w_o J_{old}(\alpha) + (1 - w_n - w_o) J_{rob}(\alpha)$$

$$w_n \geq 0, w_o \geq 0, (w_n + w_o) \leq 1$$

$$J_{new}(\alpha) = \sum_{k=1}^{N_n} \sum_{j=1}^{N_j} \frac{1}{\text{Obs}_{k,j}(\alpha)} d(\sigma_{k,j}^2(\alpha), E[\sigma_{k,j}^2(\alpha, \alpha)])$$

$$J_{rob}(\alpha) = E \left[ \left\| (\mathbf{I} - \mathbf{V}(\alpha)\mathbf{V}^T(\alpha)) \mathbf{d}^{ROB} \right\|^2 \right]$$

- $\alpha_k$ : specified model parameter
- $\alpha_j^o$ : observable from target data
- $\alpha_j$ : observable from stochastic HPRoM

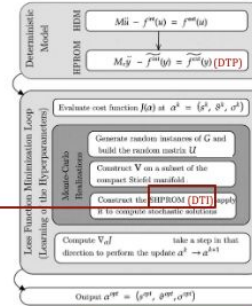
## SHPRoM

$$M_c(\alpha)\hat{y}(t, \alpha) = \hat{E}^c(y(t, \alpha)) = \hat{E}^c(\mathbf{I}^T \alpha)$$

$$M_c(\alpha) = \mathbf{V}^T(\alpha) M(\alpha) \mathbf{V}(\alpha)$$

$$\hat{E}^c(y(t, \alpha)) = \sum_{\alpha \in \mathcal{C}} \mathcal{E}^c(\mathbf{I}^T \mathbf{V}(\alpha)) \hat{f}^{opt}(\mathbf{I}^T \mathbf{V}(\alpha), \alpha)$$

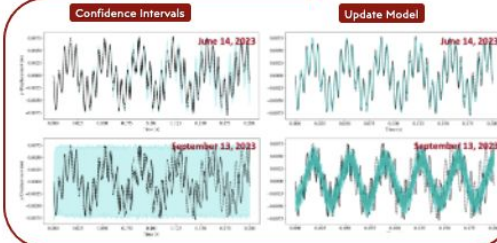
$$\hat{E}^c(\mathbf{I}^T \alpha) = \sum_{\alpha \in \mathcal{C}} \mathcal{E}^c(\mathbf{I}^T \mathbf{V}(\alpha)) \hat{f}^{opt}(\mathbf{I}^T \mathbf{V}(\alpha), \alpha)$$



## Structural Health Monitoring



## Results



## References

- Soize, C., & Farhat, C. (2017). A Nonparametric Probabilistic Approach for Quantifying Uncertainties in Low-dimensional and High-dimensional Nonlinear Models. *International Journal For Numerical Methods in Engineering*, 109(6), 837-888.
- Azzi, M. J., Chnatos, C., Avery, P., & Farhat, C. (2023). Acceleration of a Physics-Based Learning Approach for Modeling and Quantifying Model-Form Uncertainties and Performing Model Updating. *Journal of Computing and Information Science in Engineering*, 23(1), 011009.

# Satellite Ephemeris Parameterization for Lunar PNT

Marta Cortinovis, Keidai Iiyama, and Grace Gao

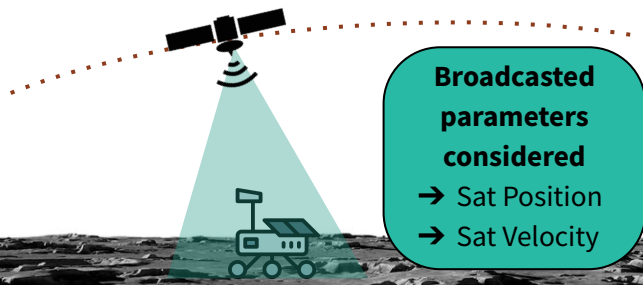


## Background

Increasing international interest in providing communication and navigation services in the lunar regime via satellite constellations.

## Objective

Develop **satellite ephemeris approximation methods** compliant with system requirements

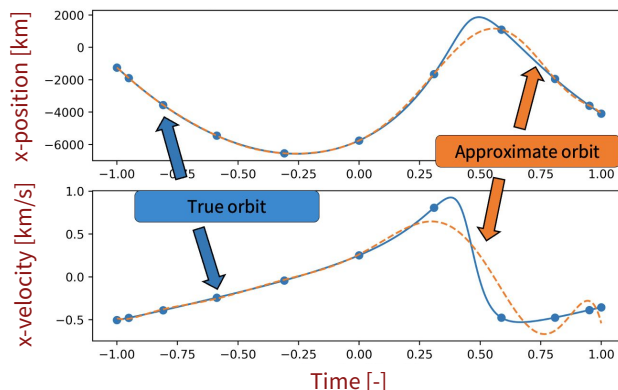


## Approach

Ephemeris coordinate-parameterization as a **constrained convex optimization problem**, comparing different surrogate models and approximation intervals

Identified **compliant Chebyshev parameterization** at low data volume for various approximation intervals

## Elliptical Lunar Frozen Orbit (ELFO) Scenario

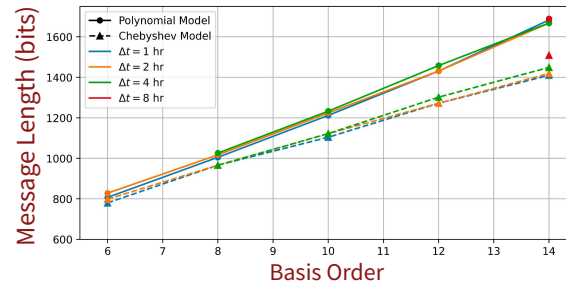


- Meet precision requirements
- Vary approximation interval
- Quantify broadcast message length

## Signal-in-Space Error Analysis

Approx. Interval	Maximum $3\sigma$ SISE <sub>pos</sub> [m]	
	Polynomial	Chebyshev
2 hrs	1.14	1.14
4 hrs	1.41	1.41
8 hrs	3.67	3.67
Requirement	< 13.34 m ( $3\sigma$ )	

## Message Length



# Low Temperature Plasma (LTP) Fluid Moment Modeling

Derek Kuldinow (PhD candidate), Daniel Troyetsky (PhD Candidate), Adnan Mansour (PhD candidate)  
Yusuke Yamashita (Postdoc), Kentaro Hara (Advisor)

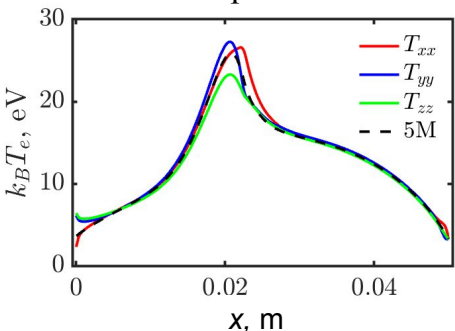


**Developing high-fidelity, robust fluid models for low temperature plasmas in industrial applications**

## 1D/2D Full-Fluid Moment (FFM) Model

- Multifluid model that solves for mass, momentum and energy including inertia, non-neutrality, etc.: Improvement over state-of-the-art, drift-diffusion models in the LTP community
- Applications: Hall effect thrusters [1] and Penning discharge [2]
- Current development: axisymmetric (cylindrical) FFM [3] for industrial applications, e.g., capacitively coupled plasmas (CCPs), spacecraft propulsion, atmospheric-pressure arc discharge

Anisotropic Plasma



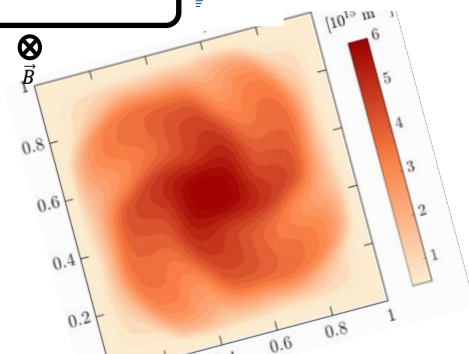
**Anisotropic temperature profile inside a Hall-effect thruster**

## 10-Moment Fluid Model

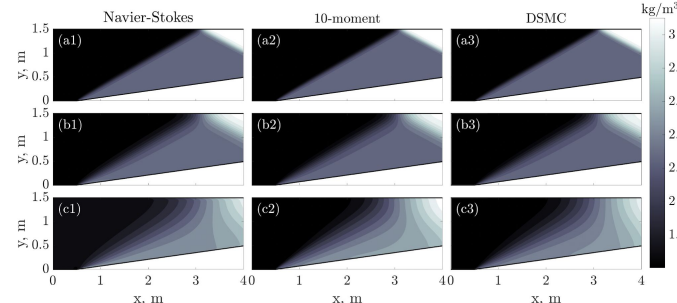
- A fluid approach that models an anisotropic pressure tensor, which can capture kinetic (non-Maxwellian velocity distribution function) effects. cf. Rarefied gas flow
- Applications: shocks, plasma sheaths, discharge [4]
- Goal: Bridge the gap between kinetic (microscopic) and fluid (macroscopic) descriptions of fluid and ionized gases (i.e., plasmas)
- Current development: plasma instabilities, turbulence, cross-field plasma discharges, rarefied gas conditions, laser-plasma interaction

### References

- 1: Sahu, Mansour, and Hara, *Phys. Plasmas* **27**, 113505 (2020)
- 2: Mansour and Hara, *Plasma Source. Sci. Tech.* **31**, 055012 (2022)
- 3: Mansour and Hara, IEP-2022-350, June 2022
- 4: Kuldinow, Mansour, Yamashita, and Hara, (*In Review*)



**Rotating spoke in a Penning discharge: Plasma density profile [2]**



**Density profile of a supersonic ramp with low collisionality [4]**

# Fueled by Purpose: Diffusion and Flattery in Self-Driving

Shounak Ray – B.S. Computer Science

Stanford Intelligent Systems Laboratory (SISL) – Prof. Mykel Kochenderfer

## Claims:

Using **diffusion** to generate synthetic driving images **improves object detection**.

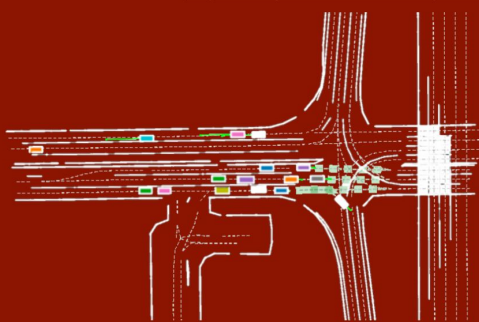
(Trained for approximately 48 hours on subset of Waymo and NuImages Perception Datasets on 2-4 V100 GPUs)



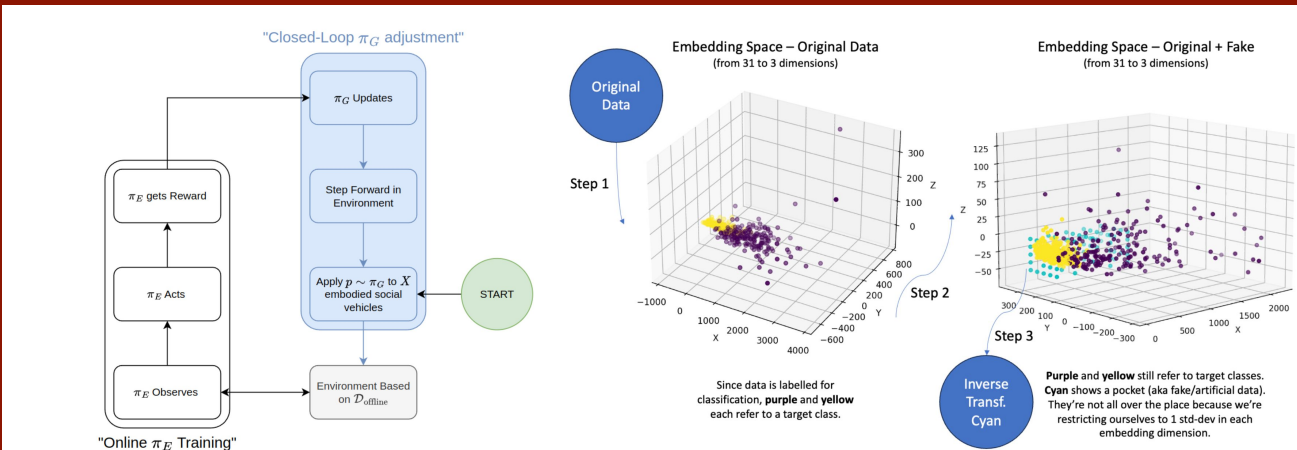
Reverse process of a latent diffusion model trained on street views and traffic scenarios. Leftmost column shows starting noise and rightmost column presents artificial images.

**Dynamically perturbing trajectories of vehicles in real-world data *strictly* to maximize reward improves robustness.**

(A single frame from a particular scenario sourced from the Waymo Motion Dataset)



Replay of a single scene from an AV dataset containing real-life vehicle trajectory recordings. An ego vehicle is set (eg. center orange) and surrounding social trajectories are perturbed.







Alboreno Voci  
PhD Candidate  
Flow Physics & Acoustics Lab  
Advisor: Sanjiva Lele



# A high-order, curvilinear multiblock solver using Legion

Alboreno Voci, Mario Di Renzo, Gianluca Iaccarino, Sanjiva Lele  
Stanford University, Department of Aeronautics and Astronautics

## Introduction

Current experiments targeting rocket propulsion for space/GEO/LEO applications are both expensive and often not as revealing regarding the detailed physics of the process. Thus, scientists turn to computational tools, where the parameters of the problem, operating conditions and uncertainties can be explicitly controlled. The drawbacks of this approach lie in the fact that the computational simulations can sometimes be as expensive as experiments and the credibility of the results is not easily verified.

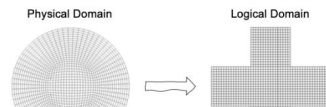
## Purpose of the Work

The goal of this work is to generalize an existing computational simulation framework, HTRV<sup>1</sup>, so that it can be used for simulations at extreme conditions. Code capabilities include (own contributions in bold)

- **Arbitrary multi-block, curvilinear structured grids**
- High temperature/enthalpy flows with dissociation/ionization
- Multi-material, multi-phase formulation
- Finite rate chemistry computed at runtime
- Integrated uncertainty quantification based on multi-fidelity ensembles
- High performance & scalability using the Legion runtime

## Method and Computational Approach

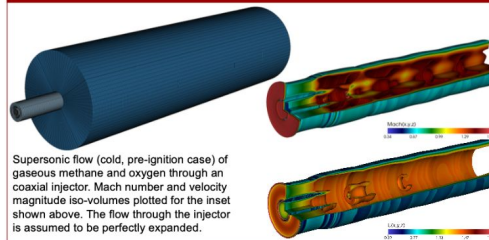
Multi-block simulations (and complex geometries in general for CFD) have been typically used in a finite volume framework. In contrast, finite difference schemes have been used for simpler topologies. Some advances are presented in Meierbachtol<sup>2</sup> et al. Here, a more general treatment for the application of high-order finite difference schemes in arbitrarily connected curvilinear structured grids is presented. The extension to a regular collection of blocks where the grid points coincide is trivial. Difficulties arise when the connections don't conform in the logical domain. To demonstrate this, a cylindrical pipe domain is considered. The logical representation of the domain involves 4 singularities, or 4 polyjunctions. These singularities require corrections to the implementation of the boundary conditions, viscous & inviscid fluxes. Results are shown for both central and shock capturing schemes.



## Acknowledgments

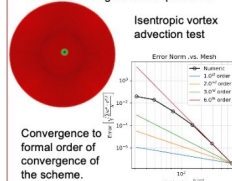
This material is based upon work supported by the Department of Energy, National Nuclear Security Administration under Award Number DE-NA0003968.

## Actual combustor mesh

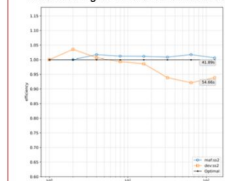


Supersonic flow (cold, pre-ignition case) of gaseous methane and oxygen through an coaxial injector. Mach number and velocity magnitude iso-volumes plotted for the inset shown above. The flow through the injector is assumed to be perfectly expanded.

### Verification using canonical problems

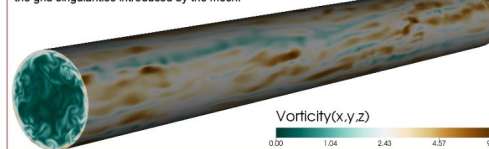


### Weak scaling for different architectures



## Turbulent pipe flow

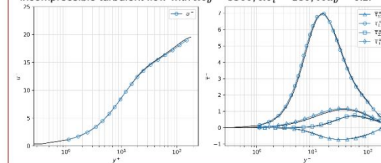
Different setups of turbulent flow in a pipe at both subsonic and supersonic Mach number were simulated and the results were compared against previously published DNS data<sup>3</sup>. The vorticity magnitude contours and other QoI don't show contamination from the grid singularities introduced by the mesh.



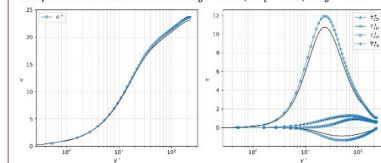
## Results

Qualitative and quantitative results are obtained using a variety of verification analytic tests, code-to-code comparisons, and experimental results. All results are found to be in accordance with the expected behavior based on a numerical analysis or within tolerances of measured data. Specifically, turbulence statistics are matched with previously published DNS within 1% in the incompressible case and within 9% for the compressible flow case. The solver maintains robustness when grid singularities are present, and it is shown that the solution is not affected by them.

Turbulence statistics (mean velocity and mean shear stresses) for an incompressible turbulent flow with  $Re_b = 5300$ ,  $Re_\tau = 180$ ,  $Ma_b = 0.2$ .



Turbulence statistics (mean velocity and mean shear stresses) for an compressible turbulent flow with  $Re_b = 6000$ ,  $Re_\tau = 224$ ,  $Ma_b = 1.5$ .



## Conclusions

The solver has been verified and validated using canonical flow problems and experimental results. More comprehensive tests of interest, such as flow over a backward facing step, turbulent pipe flow, and coaxial expanding jet. The performance of the solver is also benchmarked on both CPUs/GPUs and found to be satisfactory. Future work consists of large-scale ensembles of laser ignition combustion.

## Bibliography

- [1] Di Renzo, M., Fu, L., & Urzay, J. (2020). Computer Physics Communications.
- [2] Meierbachtol, Collin S., et al. (2017). J. Comput. Phys.
- [3] Modesti, D., & Pirozzoli, S. (2019). Int. J. Fluid Heat Flow.

## Further Information

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## Semantic Anomalies

**Semantic Anomalies:** System-level out-of-distribution (OOD) inputs that arise from an unusual or “tricky” combination of individually in-distribution observations.

### Real-World Examples:

#### Stop Sign Imagery on a Billboard



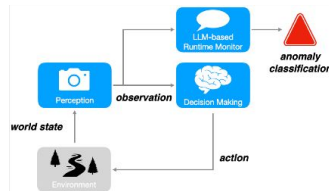
#### Truck Carrying Traffic Lights



## Anomaly Detection Framework

Thanks to the sheer scale of their training datasets, Large Language Model (LLM):

- (1) demonstrate **strong automated reasoning performance** and
- (2) **possess contextual understanding** in alignment with human intuition.



## Autonomous Vehicle Monitoring

Vehicle Perception:

Object Detector

Scene Description:

- > truck
- > tree
- > street light
- > traffic sign
- > truck carrying a traffic light

Prompt Template (Paraphrased):

I am the fault monitor for a vision-based autonomous vehicle. My job is to analyze the vehicle's observations and identify anything that could cause the vehicle to take actions that are unsafe, unpredictable or violate traffic rules.

I must consider whether each observation:

- is commonly seen while driving,
- has the capacity to influence the vehicle's driving, or
- can compromise the vehicle's safety.

The vehicle is driving on the road and observes:

•Scene Descriptions•

Here are the results of my analysis:

LLM Response (Excerpted):

\*Traffic Sign:

Can this cause the vehicle to make unpredictable or unsafe maneuvers? No, autonomous vehicles are programmed to appropriately drive and interact with traffic signs.  
Classification: Normal.

\*Truck carrying a traffic light:

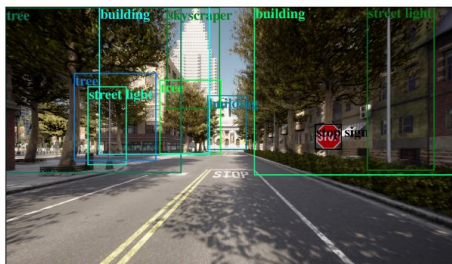
Can this cause the vehicle to make unpredictable or unsafe maneuvers? Yes, this could deceive the autonomous vehicle into driving forward when it should otherwise be stopped (e.g., at a red light).  
Classification: Anomaly.

Object detector generates scene description

Chain-of-thought style prompt structures LLM reasoning.

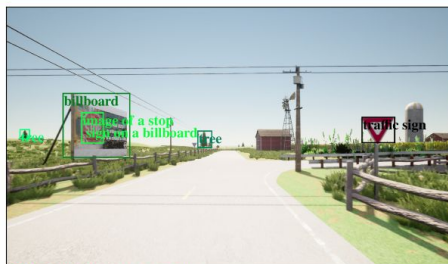
Monitor accurately recognizes the unusual context.

## Qualitative Results



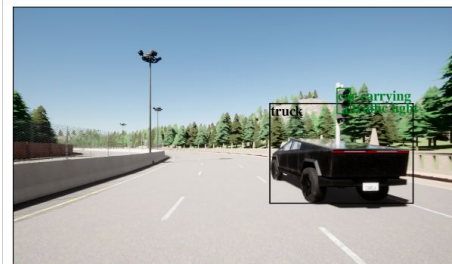
Classification: Normal.

Reasoning: “The vehicle can drive safely in the presence of stop signs.”



Classification: Anomaly.

Reasoning: “The autonomous vehicle may mistake the image of the stop sign for an actual stop sign, which could deceive it into stopping when it should otherwise be driving.”



Classification: Anomaly.

Reasoning: “The autonomous vehicle may mistake the traffic light for a real traffic signal, which could deceive it into driving forward when it should otherwise be stopped (e.g., at a red light).”

# Shape reconstruction of large multi-stable apertures through state sensing

Reconfigurable & Active Structures Lab: Enquan Chew (PhD Candidate), Prof. Maria Sakovsky

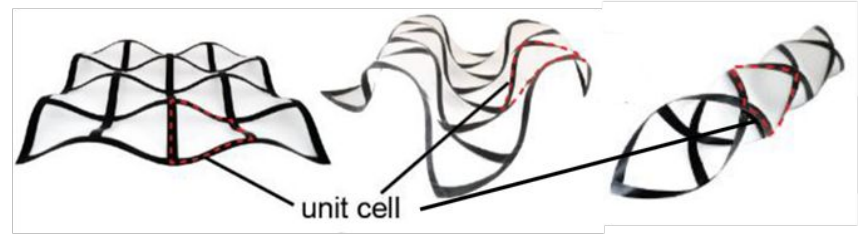
Increasingly larger apertures desired for increased performance of space-based phased array antennas

Challenges faced for lightweight architecture

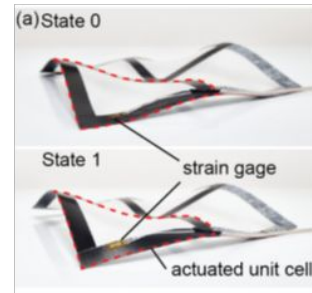
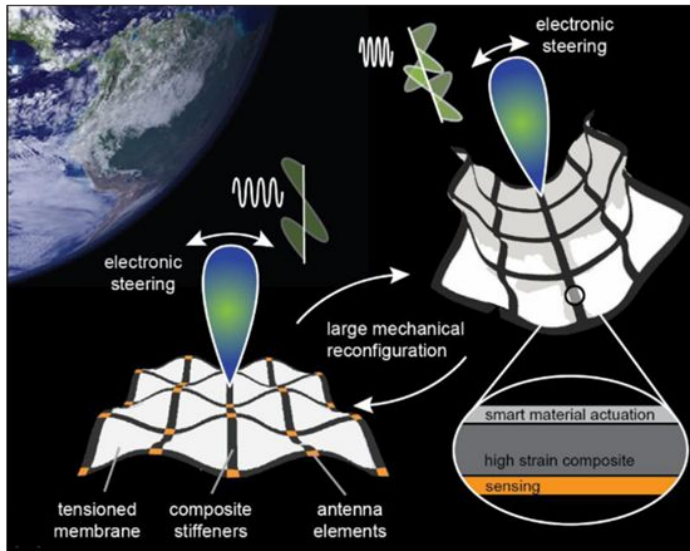
- Thermal and vibration disturbances
- Real time measurement and compensation required

Multi-stable surfaces

- Finite number of discrete stable states



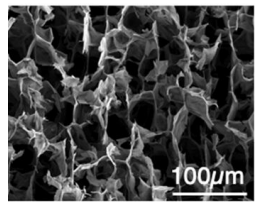
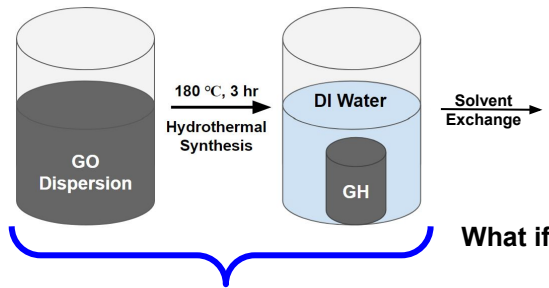
**Objective: Realize shape reconstruction of large multi-stable apertures through state sensing**



# Graphene Aerogel in Microgravity: Electrical Property Characterization

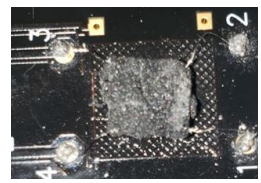
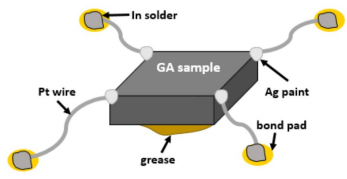


Synthesizing GA from a graphene hydrogel (GH) starts with a hydrothermal reduction:



What if we completed this first step in space?

Preliminary Electrical Characterization: van der Pauw Method



Current/Future Electrical Characterization: Electrochemical

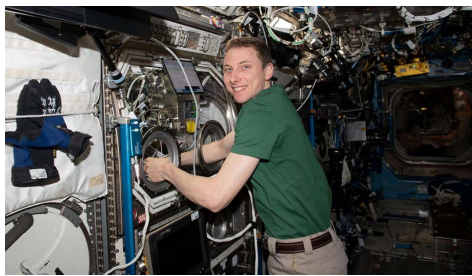
## Earth-synthesized graphene aerogel

- Buoyancy induced effects
- Sedimentation & stratification
- Anisotropic properties



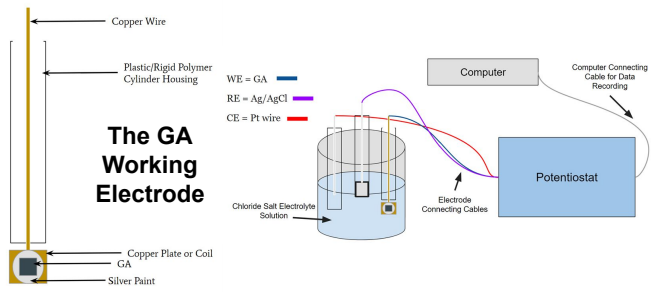
## Microgravity-synthesized graphene aerogel

- Brownian motion driven effects
- More uniform microstructure
- Isotropic properties



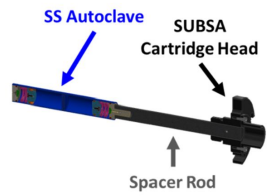
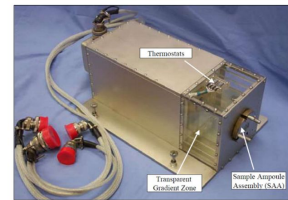
Astronaut Woody Hoburg completing our experiment!

Image courtesy of NASA



- ### Applications
- Sensor technology
  - Capacitors and batteries
  - EM wave absorption
  - Thermal insulation for spacecraft

Synthesis Hardware on the ISS



NASA's SUBSA (solidification using a baffle in sealed ampoules) furnace managed by Techshot, Inc., a RedWire Company.





# Detecting Space Based Interference on GNSS Signals

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